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9

10 Original Article / Technical note

11 **A holistic approach to study the temporal variability in gait.**

12

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27 **Abstract**

28 Movement variability has become an important field of research and has been studied to gain a  
29 better understanding of the stability or the neuro-muscular control of human movements. In  
30 addition to studies investigating “amplitude variability” there are a growing number of studies  
31 assessing the “temporal variability” in movements by applying non-linear analysis techniques.  
32 One limitation of the studies available to date is that they quantify variability features in specific,  
33 pre-selected biomechanical or physiological variables. In many cases it remains unclear if and  
34 to what degree these pre-selected variables quantify characteristics of the whole body  
35 movement. This technical note proposes to combine two analysis techniques that have already  
36 been applied for gait analysis in order to quantify variability features in walking with variables  
37 whose significance for the whole movements are known. Gait patterns were recorded using a  
38 full-body marker set on the subjects whose movements were captured with a standard motion  
39 tracing system. For each time frame the coordinates of all markers were interpreted as a high-  
40 dimensional “posture vector”. A principal component analysis (PCA) conducted on these  
41 posture vectors identified the main one-dimensional movement components of walking.  
42 Temporal variability of gait was then quantified by calculating the maximum Lyapunov Exponent  
43 (LyE) of these main movement components. The effectiveness of this approach was  
44 demonstrated by determining differences in temporal variability between walking in unstable  
45 shoes and walking in a normal athletic-type control shoe. Several additional conceptual and  
46 practical advantages of this combination of analysis methods were discussed.

47

## 48 **Introduction**

49 Analysis of movement variability has become an important field in motor-control and  
50 biomechanical research. Bernstein pointed out that for any given motor task there are an infinite  
51 number of possible solutions (Bernstein, 1967). He attributed this observation to the fact that the  
52 multitude of joints and muscles in the human body create redundant degrees of freedom.  
53 Variability in movements is therefore not only caused by external perturbations, but also needs  
54 to be considered as an inherent property of the system itself. Changes in movement variability  
55 might be a sign of injury (Cavanaugh, Guskiewicz, & Stergiou, 2005; Stergiou, Harbourne, &  
56 Cavanaugh, 2006; Harbourne & Stergiou, 2009), disorder (Hausdorff, Cudkowicz, Firtion, Wei,  
57 & Goldberger, 1998; Moraiti, Stergiou, Ristanis, & Georgoulis, 2007; Stolze et al., 2001;  
58 Ebersbach et al., 1999; Rosengren et al., 2009; Webster, Merory, & Wittwer, 2006; Dingwell &  
59 Cusumano, 2000) or aging of the neuro-muscular system (Kang & Dingwell, 2008; Verrel,  
60 Lövdén, & Lindenberger, 2012; Verrel, Lövdén, Schellenbach, Schaefer, & Lindenberger, 2009;  
61 Buzzi, Stergiou, Kurz, Hageman, & Heidel, 2003; Callisaya, Blizzard, Schmidt, McGinley, &  
62 Srikanth, 2010; Brach, Studenski, Perera, VanSwearingen, & Newman, 2007).

63 The term “variability” is used with different meaning in different contexts. It is therefore important  
64 to specify what features of variability are analyzed. In general, this manuscript studies aspects  
65 of the intra-subject motion variability. Inter-subject variability, while related to the topic of this  
66 study, will not be discussed further. In most fields of sciences the term “variability” refers to any  
67 kind of variations in an observed variable, however, in the field of motor-control “variability” is  
68 often used in a very specific meaning as a quantification of the variability in the amplitude of a  
69 time series. If a time series is stationary, “amplitude variability” can be quantified by descriptive  
70 statistical measures such as standard deviation (Dingwell, Cusumano, Cavanagh, & Sternad,  
71 2001). Aspects of temporal variations in gait variables have been quantified by different non-  
72 linear analysis methods such as the *maximum Lyapunov Exponent* (LyE) (Jordan, Challis,

73 Cusumano, & Newell, 2009; Terrier & Deriaz, 2011; England & Granata, 2007; Dingwell &  
74 Marin, 2006; Dingwell & Cusumano, 2000; Bruijn et al., 2009), approximate entropy (ApEn)  
75 (Goldberger, Peng, & Lipsitz, 2002; Georgoulis, Moraiti, Ristanis, & Stergiou, 2006), or Poincare  
76 analyses (Granata & Lockhart, 2008; Dingwell, Robb, Troy, & Grabiner, 2008; Dingwell & Kang,  
77 2007). In this study the *maximum Lyapunov Exponent* (LyE) was used. LyE quantifies how fast  
78 the waveform of a time series changes from step cycle to step cycle. Thus, in a sense, LyE  
79 quantifies the “predicatability” of the time series. A common interpretation is also that LyE is a  
80 measure of the “dynamic stability” of the process that produced the analysed time series  
81 (Dingwell et al., 2001; Segal, Orendurff, Czerniecki, Shofer, & Klute, 2008).

82         Studies employing nonlinear approaches to study temporal variability features in gait  
83 have so far been conducted on specific pre-selected variables, for example, joint angles (ankle,  
84 knee, hip) or trunk movements (Dingwell & Cusumano, 2000; Buzzi et al., 2003; Dingwell &  
85 Kang, 2007; Park, Son, Kim, & Seo, 2008; Segal et al., 2008; Nessler, De Leone, & Gilliland,  
86 2009; Son, Park, & Park, 2009; Myers, Stergiou, Pipinos, & Johanning, 2010). However, in  
87 many cases it remains unclear if and to what degree the temporal variation of such pre-selected  
88 variables might be representative for the movement characteristics of the whole body. Pre-  
89 selection of variables also carries a certain risk of investigator bias influencing the study and it is  
90 possible that other important variability features, which would be visible in variables not selected  
91 for analysis, might be missed.

92         The purpose of this technical note was the introduction of a method to study aspects of the  
93 variability in the movement of the whole loco-motor system that does not require the pre-  
94 selection of specific variables. The underlying idea of the approach presented here was to first  
95 capture the subjects’ multi-segment gait movements with a full-body marker set tracked by a  
96 standard motion capture system. These multi-segment movement patterns were decomposed  
97 into one-dimensional movement components using a principle component analysis (PCA)

98 according to a method described by Troje (2002), Daffertshofer and colleagues (2004), or Verrel  
99 and colleagues (2009). The temporal variability features of gait were then quantified by  
100 calculating the LyE for these principal movement components. It is demonstrated in this paper  
101 that the proposed method is able to distinguish temporal variability characteristics when walking  
102 in two types of footwear.

## 103 **Methods**

### 104 Data collection

105 Twenty healthy subjects volunteered for this study (6 female, 14 male; age  $24 \pm 2$ ;  
106 weight  $71 \pm 11$  kg; height  $1.77 \pm 0.04$  m [mean  $\pm$  SD]). All participants gave informed written  
107 consent, and the study was approved by the appropriate Institutional Review Board. None of the  
108 subjects had any known orthopedic or neurological conditions that would affect their gait.

109 All subjects walked on a treadmill at a pre-determined self-selected speed. To select the  
110 speed, subjects were first instructed that they should choose a pace as if they were late for an  
111 appointment, but at which they could walk for 20 minutes. Then they walked on a treadmill while  
112 the speed was stepwise increased by the experimenter until the subject indicated that the speed  
113 was too high. From this point the speed was successively reduced until the subject felt confident  
114 that he or she could maintain this pace for 20 min. This procedure was followed by 5-minute  
115 warm-up walking at the selected speed. If the subject felt it was necessary, small adjustments of  
116 the speed were allowed during the first 2 minutes. The final walking speed was on average  $3.8$   
117  $\pm 0.1$  m/s.

118 For this technical note two walking trials were analyzed, one with subjects walking in an  
119 athletic-type casual shoe ("Ekiden 100" manufactured by Kalenji®, Decathlon SA., France) and  
120 one with subjects walking in an unstable shoe ("Mwalk" manufactured by Masai Barefoot  
121 Technology Inc. (MBT™), Switzerland). Each trial consisted of an acclimatization period of 30

122 seconds, then a measurement of 100 seconds was collected. Subjects were informed of the  
123 beginning and the end of the data collection period and were asked to focus their gaze on a  
124 target in front of them, however, for safety reasons and to allow the subjects to verify their  
125 position on the treadmill it had no consequences if a subject looked away from the target.

126 The subjects' individual walking patterns were recorded using a full-body marker set  
127 consisting of 28 markers placed on bony landmarks on all body segments (Figure 1).  
128 Specifically, the markers were placed on the left and right lateral malleolus, lateral epicondyle of  
129 the knee, anterior and posterior superior iliac spine, acromio-clavicular joint, lateral epicondyle  
130 of the elbow joint, both sides of the wrist joint, on the sternum, clavicle, 7th cervical  
131 vertebrae, and four markers were attached to a head band. Additional markers were placed on  
132 the shoe surfaces as close as possible to the calcaneus and on the second metatarsal head.  
133 The other markers were not changed between conditions. The three-dimensional marker  
134 trajectories were acquired at a sampling rate of 240 Hz using a standard eight camera motion  
135 capture system (Motion Analysis Corporation, Santa Rosa CA, USA). EVa Real-Time Software  
136 (EVaRT, Motion Analysis Corporation, Santa Rosa CA, USA) was used for real-time motion  
137 capture and for post-processing of the marker trajectories. The recorded spatial coordinates  
138 were not filtered during post-processing to retain an accurate representation of the variability  
139 within the locomotor system.

#### 140 Outline of the data analysis steps

141 The data analysis consisted of the following main steps. 1) Detection of gait cycles from  
142 the vertical position of the heel marker and selection of 65 consecutive cycles for further  
143 analysis; 2) Principal component analysis (PCA) on posture vectors defined with all marker data  
144 to identify the main movement patterns of walking ("*principal movements*"); 3) Transformation of  
145 the posture vectors onto the first five principal component vectors, which contained >95% of the



146 entire postural variability; 4) Analysis of the *temporal variability* by analyzing the time series  
147 formed by the principal component scores.

#### 148 Principal movement components of walking

149 PCA is a statistical technique frequently used to reduce the number of variables  
150 necessary to explain a process (e.g. locomotion) while retaining most of the variation present in  
151 the original data set (Jolliffe, 2002). PCA is based on an eigenvalue decomposition of the  
152 covariance matrix of the data set into eigenvectors called principal component vectors (PCs).  
153 These components are arranged in decreasing order of their sample variance. Typically the  
154 majority of variation is contained in the first few PCs. Omitting higher order principal  
155 components allows to reduce the number of variables that describe the system while retaining  
156 of most of the variability, i.e. information.

157 In this study, the PCA was applied for the analysis of gait patterns similarly to the  
158 method described in detail by Troje (2002), Daffertshofer et al. (2004) or Verrel et al.(2009).  
159 Specifically, each trial returned a matrix of 84 spatial coordinates (28 3D marker positions) in  
160 24000 time frames (100 seconds collected at 240Hz) of which the time frames corresponding to  
161 65 consecutive steps were selected. Each row of the matrix was interpreted as an 84-  
162 dimensional "*posture vector*" representing all available information about the subject's posture in  
163 the given time frame. The *mean posture vector* calculated over all 65 steps was subtracted from  
164 each row of this matrix but no other normalization was performed.

165 Performing a PCA on this matrix yielded a) orthogonal principal component vectors,  $PC_k$ ,  
166 in the direction of the largest variances in *posture vectors* (Figure 2 A,B,C and video files 1 to 3);  
167 b) eigen values,  $EV_k$ , which quantified the amount of variance explained by the corresponding  
168  $PC_k$ ; c) coefficients  $c_k(t)$  (in some publications also called *scores*) obtained by projecting each  
169 posture vector onto the  $PC_k$  (Figure 2 D,E,F). Applying the PCA to walking decomposes this  
170 complex multi-segment movement into one-dimensional movement components that originate

171 from a mean posture, i.e. from a mean marker configuration. The 84-dimensional  $PC_k$ -vectors  
172 determine for each movement component  $k$  in what direction the markers move. The  
173 coefficients  $c_k(t)$  quantify for each time point  $t$  how far the momentary posture (=momentary  
174 marker configuration) deviates from the mean posture in the direction of the associated  $PC_k$ .  
175 The  $EV_k$  quantify how much deviations from the mean posture in the direction of the associated  
176  $PC_k$  were observed during the whole trial. The  $EV_k$  were expressed as percentage of the sum of  
177 all 84  $EV_k$ s. Thus they quantify how much of the total variance in posture vectors observed  
178 during the trial occurred in the associated  $PC_k$  (Troje, 2002; Verrel et al., 2009; Daffertshofer et  
179 al., 2004). For simplicity we refer to these one-dimensional movement components as "*principal*  
180 *movements* ( $PM_k$ )". The PCA calculations conducted in this study were implemented in Matlab  
181 (MathWorks Inc., Natic, MA, USA).

#### 182 Assessment of *temporal variability* using the maximum Lyapunov exponent (LyE)

183 The temporal characteristics of the whole body movement patterns of walking were then  
184 analyzed by assessing the temporal variability characteristics of the time series  $c_k(t)$ . The LyE  
185 was determined by first constructing a state space representation of the time series. Thereto,  
186 the time delay  $\tau$  was determined by an algorithm finding the first minimum of the average mutual  
187 information (AMI) as described by Fraser and Swinney (Fraser & Swinney, 1986). The  
188 appropriate embedding dimension was determined using a false nearest neighbor algorithm  
189 (Kantz & Schreiber, 1997). An embedding dimension of  $n=5$  minimized the number of false  
190 nearest neighbors in most time series and was therefore used for the analysis of all principal  
191 movements in all trials. Following reconstruction of the state space (Figure 2 G,H,I), mean  
192 divergence curves and LyE values were calculated for the time series based on Kantz's  
193 algorithm (Hegger & Kantz, 1999; Kantz, 1994). Kantz's algorithm is conceptually equal to the  
194 algorithm proposed by Rosenstein et al. (Rosenstein, Collins, & De Luca, 1993) and is

195 implemented in the software package TISEAN (version 3.0.1) (Hegger & Kantz, 1999) which  
196 was combined with the Matlab codes used for the calculating the PMs.

## 197 **Results**

198           The variance in posture vectors represented in each of the first five PMs is listed in  
199 Table 1 for both types of test shoes. No statistical differences between the two test shoes were  
200 found. For all subjects, the first three principal components represented the same type of  
201 movement in both test shoe conditions (Figure 2 and video files 1 to 3 give a graphic  
202 visualization).  $PM_1$  represented the posture variation due to anterior-posterior arm and leg  
203 swing.  $PM_2$  quantified a synchronous flexion-extension of both knees with an in-phase vertical  
204 movement of the upper body.  $PM_3$  quantified an asynchronous flexion of the knee with an in-  
205 phase medial shift of the upper body (and thus the body weight) onto the stance leg. Higher  
206 order movement components represented adjustments of these basic movement components.  
207 For example,  $PC_4$  and  $PC_5$  portrayed small additional ankle, knee and elbow flexion-extension  
208 movements in most subjects. However, the movement components represented by the PMs  
209 became increasingly subject specific with increasing PM order.

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216 Table 1 Eigen value spectrum of the first five principal movement components of  
 217 walking when wearing a normal athletic shoe or an unstable shoe.

Principal movement	EV normal shoe	EV unstable shoe	paired T-test
	Mean (SD)	Mean (SD)	p-value
PM <sub>1</sub>	84.2% (4.3%)	84.2% (3.6%)	0.98
PM <sub>2</sub>	6.6% (3.7%)	6.3% (3.2%)	0.80
PM <sub>3</sub>	3.2% (0.3%)	3.2% (0.4%)	0.52
PM <sub>4</sub>	2.3% (0.8%)	2.4% (0.7%)	0.41
PM <sub>5</sub>	1.3% (0.5%)	1.3% (0.4%)	0.58

218

219 The LyE values characterizing the temporal variability of the first five PMs are listed in  
 220 Table 2 for both types of footwear. The difference between walking in a normal shoe and  
 221 walking in an unstable shoe was significant in PM<sub>1</sub> and PM<sub>2</sub>. In higher movement components  
 222 no significant differences were found.

223 Table 2 Maximum Lyapunov Exponent (LyE) determined for the first three principal  
 224 movement components of walking in different test shoes.

Principal movement	EV normal shoe	EV unstable shoe	paired T-test
	Mean (SD)	Mean (SD)	p-value
PM <sub>1</sub>	0.063 (0.007)	0.138 (0.045)	<b>&lt;0.001</b> *
PM <sub>2</sub>	0.095 (0.018)	0.122 (0.038)	<b>0.020</b> *
PM <sub>3</sub>	0.095 (0.012)	0.093 (0.015)	0.633
PM <sub>4</sub>	0.099 (0.021)	0.097 (0.022)	0.866
PM <sub>5</sub>	0.105 (0.029)	0.115 (0.030)	0.235

225 \* indicates significance at the  $\alpha = 0.05$  level

226 **Discussion**

227 The combination of a PCA decomposition of the main movement patterns of gait with non-linear  
228 analysis methods to analyze temporal variability characteristics was able to identify differences  
229 in the temporal variability characteristics when walking in an unstable shoe as compared to  
230 walking in a normal athletic-type control shoe. The analysis approach developed in this study  
231 has, in the opinion of the authors, several important advantages as compared to previously  
232 employed analysis methods. First, the contribution of each principal movement component to  
233 the entire postural variability in walking is known since it is directly quantified by the normalized  
234 eigenvalues (Table 1). Quantifying the temporal variability of these movement components  
235 rather than that of selected variables such as joint angles or selected marker positions therefore  
236 has the advantage that the significance of these variables for the behavior of the whole system  
237 is known. Moreover, the first three PMs quantified similar movements in all subjects and the  
238 functional implications of these PMs for the whole motion can directly be assessed.  $PM_1$  was  
239 the main contributor to forward propagation,  $PM_2$  quantified a vertical motion, and  $PM_3$  a lateral  
240 weight shift during gait (video files 1 to 3). Considering these functional implications it will  
241 become easier in future studies to develop directional hypotheses for how external factors, such  
242 as unstable shoes, might influence the variability characteristics of the gait.

243 Secondly, PCA is an unbiased, data-driven method to identify correlations in the multiple  
244 movement variables that can be observed in gait (Daffertshofer et al., 2004). Quantifying  
245 variability characteristics in the PMs rather than investigating variability in selected variables is  
246 therefore also conceptually a better approach when studying motor control questions.

247 Finally, non-linear analysis methods are known to be sensitive to noise (Argyris, Andreadis,  
248 Pavlos, & Athanasiou, 1998). However, random noise will affect different marker coordinates in  
249 an uncorrelated manner. Applying a PCA to the dataset containing all marker positions has  
250 therefore also the advantage that random noise will have a small effect on principal components

251 with large eigenvalues (Romero, 2010). The first few PMs, which are of particular interest for the  
252 analysis of the system's behavior, are therefore less affected by noise than the original marker  
253 coordinates or than any variable that is calculated from only a few markers. Assessing temporal  
254 variability features in human movement in the *principal movements* therefore also has the  
255 practical advantage of being less affected by measurement noise and therefore more sensitive  
256 for differences due to the test conditions.

### 257 Limitations and other considerations

258 One limitation of the approach outlined in this study is that PCA decomposes the movements  
259 into linear movement components while the actual segment movements are typically rotations  
260 and thus non-linear. One consequence of the linear movement decomposition is that at least  
261 two linear variables (PMs) are needed to quantify a rotational motion. The decomposition  
262 provided by the PCA will therefore not yield functionally independent movement components  
263 and an appropriate non-linear decomposition method might be able to reduce the number of  
264 PMs that are necessary to accurately describe the entire movement.

265 The chosen marker set and the normalization procedures will influence the resultant PMs and  
266 the relative postural variability that each PM explains. While PM<sub>1</sub> represented the same  
267 movement component of walking in all studies that we are aware of, the movements  
268 represented by PM<sub>2</sub> and higher PMs observed in this study differed from those reported by  
269 Verrel and colleagues (2009), who performed an additional normalization step in which the  
270 subject's position on the treadmill was removed before entering the analysis. We abstained from  
271 additional normalization steps, such as the removal of relative movements on the treadmill  
272 (Verrel et al, 2009) or the normalization to equal variance (Daffertshofer et al., 2004), because  
273 they distort the actual variability observed in the marker positions and would thus also affect the  
274 assessment of the temporal variability in the gait patterns. However, the EV observed in this  
275 study can be directly compared to the results of Troje (2002) who also did not normalize the

276 marker positions before applying the PCA. We found that  $EV_1$  agreed very well with Troje's  
277 results, however, the higher order EV differed between the two studies. We speculate that  
278 differences in the marker sets might be responsible for these discrepancies.

## 279 Conclusions

280 For the analysis of temporal variability characteristics of the whole neuro-muscular system we  
281 combined a common non-linear analysis method (calculating LyE) with the PCA decomposition  
282 of gait patterns proposed by Troje (2002) or Daffertshofer (2004). This approach was effective in  
283 identifying differences between unstable shoes and normal shoes. The combination of these  
284 analysis methods has several conceptual and practical advantages as compared to the analysis  
285 of temporal variability in pre-selected variables such as individual marker positions of joint  
286 angles.

287

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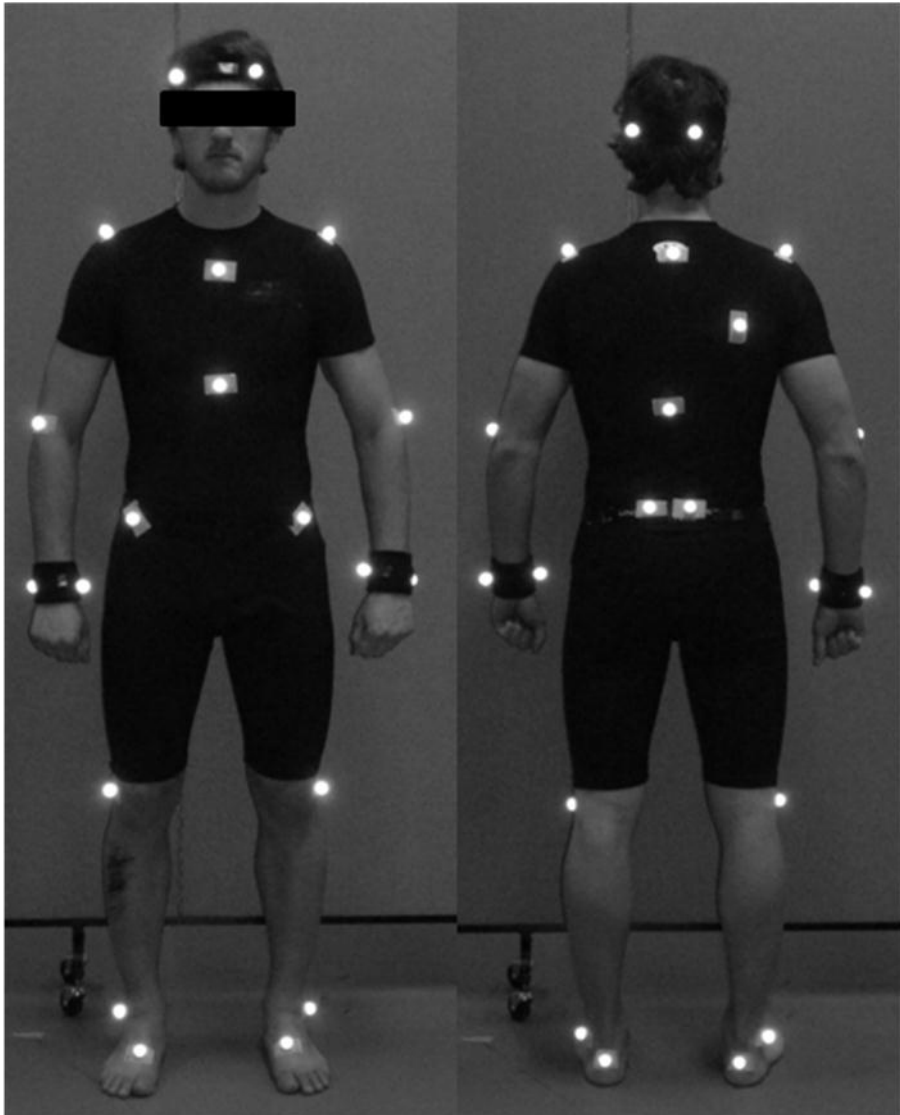
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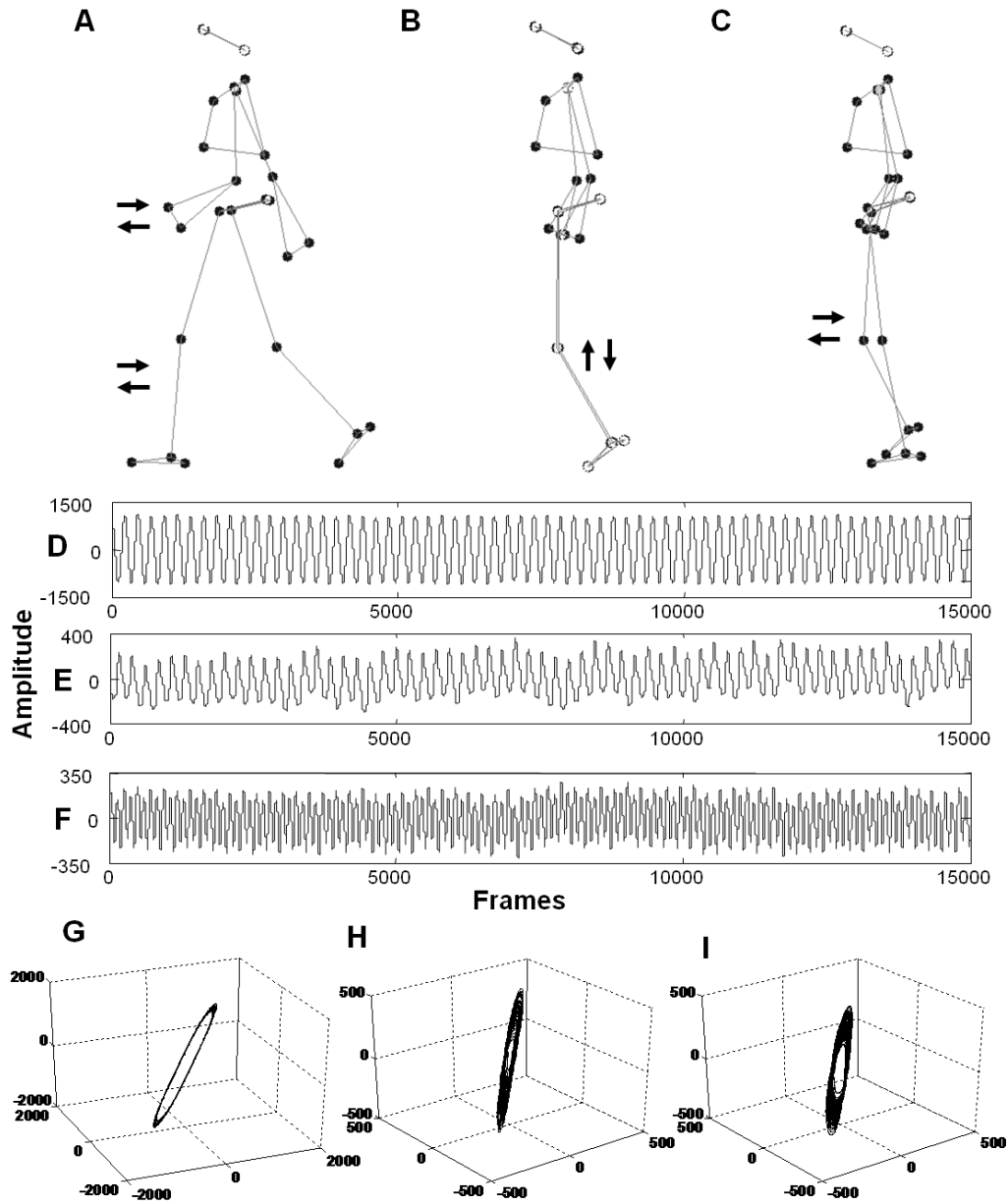
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398 Figure 1. Positions of twenty-eight reflective markers for the quantification of the whole-body  
399 kinematics.



400

401 Figure 2. (A), (B) and (C) illustrate the main movement patterns corresponding to the first three  
 402 principal components calculated from the marker trajectories recorded from a representative  
 403 subject during walking. (D), (E), and (F) represent the time series obtained from the projection of  
 404 all posture vectors onto the first three principle components. (G), (H), (I) show a three  
 405 dimensional representation of the state space trajectories of the first three principal movements.

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